

# Mixture Differential Cryptanalysis: a New Approach to Distinguishers and Attacks on round-reduced AES

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March, 2019

# Motivation

At Eurocrypt 2017, the first secret-key distinguisher for 5-round AES - based on the **multiple-of-8** property - has been presented.

However, *it seems rather hard to implement a key-recovery attack different than brute-force like using such a distinguisher:*  
can this new observation lead to attacks on AES which are competitive w.r.t. previously known results?

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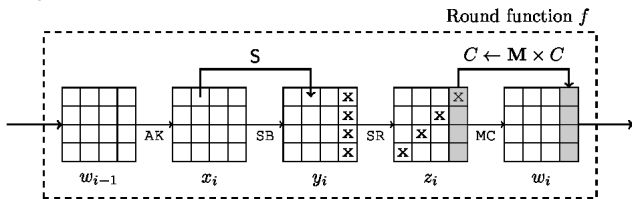
# Part I

## AES Design and the “Multiple-of-8” Property

# AES

High-level description of **AES** [DR02]:

- block cipher based on a design principle known as *substitution-permutation network*;
- block size of 128 bits = 16 bytes, organized in a  $4 \times 4$  matrix;
- key size of 128/192/256 bits & 10/12/14 rounds:



Source-code of the Figure – by Jérémy Jean – copied from <https://www.iacr.org/authors/tikz/>

## “Multiple-of-8” property for 5-round AES [GRR17b]

Assume 5-round AES without the final MixColumns operation.  
Consider a set of  $2^{32}$  chosen plaintexts with one active diagonal

$$\begin{bmatrix} A & C & C & C \\ C & A & C & C \\ C & C & A & C \\ C & C & C & A \end{bmatrix}$$

The number of *different* pairs of ciphertexts which are equal in one (fixed) anti-diagonal

$$\begin{bmatrix} 0 & ? & ? & ? \\ ? & ? & ? & 0 \\ ? & ? & 0 & ? \\ ? & 0 & ? & ? \end{bmatrix}$$

is a multiple of 8 with probability 1 independent of the secret key, of the details of S-Box and of MixColumns matrix.

## Multiple-of-8 Property– Formal Theorem

Consider  $2^{32 \cdot |I|}$  plaintexts with  $|I|$  active diagonals (namely, in an affine space  $\mathcal{D}_I \oplus a$ ) and the corresponding ciphertexts after 5 rounds, i.e.  $(p^i, c^i \equiv R^5(p^i))$  for  $i = 0, \dots, 2^{32 \cdot |I|} - 1$  where  $p^i \in \mathcal{D}_I \oplus a$ .

### Theorem (Eurocrypt 2017)

*For a fixed  $J \subseteq \{0, 1, 2, 3\}$ , let  $n$  be the number of different pairs of ciphertexts  $(c^i, c^j)$  for  $i \neq j$  such that  $c^i \oplus c^j$  are equal in  $4 - |J|$  anti-diagonals (namely,  $c^i \oplus c^j \in \mathcal{M}_J$ ):*

$$n := |\{(p^i, c^i), (p^j, c^j) \mid \forall p^i, p^j \in \mathcal{D}_I \oplus a, p^i < p^j \text{ and } c^i \oplus c^j \in \mathcal{M}_J\}|.$$

*The number  $n$  is a multiple of 8 independent of the secret key, of the details of S-Box and of MixColumns matrix.*

# What about a Key-Recovery Attack?

What happens if we extend the previous distinguisher *into a key-recovery attack*? E.g.

$$\mathcal{D}_I \oplus a \xrightarrow[\text{prob. } 1]{R^5(\cdot)} \text{multiple-of-8} \xleftarrow[\text{key-guessing}]{R^{-1}(\cdot)} \text{ciphertexts}$$

**Problem:** we need to guess the **entire** final round-key in order to check the property

“number of pairs of ciphertexts  $(c^i, c^j)$  s.t.

$$\left\{ (c^i, c^j) \mid i < j \text{ and } R^{-1}(c^i) \oplus R^{-1}(c^j) = MC^{-1} \times \begin{bmatrix} 0 & ? & ? & ? \\ ? & ? & ? & 0 \\ ? & ? & 0 & ? \\ ? & 0 & ? & ? \end{bmatrix} \right\}$$

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## Part II

# Mixture Differential Cryptanalysis

# From Multiple-of-8 to Mixture Diff. Cryptanalysis

*Why does the “multiple-of-8” property hold? Given a pair of plaintexts  $(p^1, p^2)$  s.t.  $R^5(p^1) \oplus R^5(p^2) \in \mathcal{M}$ , then other pairs of texts  $(q^1, q^2)$  have the same property ( $R^5(q^1) \oplus R^5(q^2) \in \mathcal{M}$ ), where the pairs  $(p^1, p^2)$  and  $(q^1, q^2)$  are not independent.*

Instead of limiting ourselves to count the number of collisions and check that it is a multiple of 8, *the idea is to check the relationships between the variables that generate the pairs of plaintexts  $(p^1, p^2)$  and  $(q^1, q^2)$ .*

**Mixture Differential Cryptanalysis:** a way to translate the “multiple-of-8” 5-round distinguisher into a simpler and more convenient one (though, on a smaller number of rounds).

## From Multiple-of-8 to Mixture Diff. Cryptanalysis

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Instead of limiting ourselves to count the number of collisions and check that it is a multiple of 8, *the idea is to **check the relationships** between the variables that generate the pairs of plaintexts  $(p^1, p^2)$  and  $(q^1, q^2)$ .*

**Mixture Differential Cryptanalysis:** a way to translate the “multiple-of-8” 5-round distinguisher into a simpler and more convenient one (though, on a smaller number of rounds).

# Mixture Diff. Cryptanalysis – 1st Case (1/2)

Consider  $p^1, p^2 \in \mathcal{C}_0 \oplus a$ :

$$p^1 = a \oplus \begin{bmatrix} x^1 & 0 & 0 & 0 \\ y^1 & 0 & 0 & 0 \\ z^1 & 0 & 0 & 0 \\ w^1 & 0 & 0 & 0 \end{bmatrix}, \quad p^2 = a \oplus \begin{bmatrix} x^2 & 0 & 0 & 0 \\ y^2 & 0 & 0 & 0 \\ z^2 & 0 & 0 & 0 \\ w^2 & 0 & 0 & 0 \end{bmatrix}$$

where  $x^1 \neq x^2$ ,  $y^1 \neq y^2$ ,  $z^1 \neq z^2$  and  $w^1 \neq w^2$ .

For the following:

$$p^1 \equiv (x^1, y^1, z^1, w^1) \quad \text{and} \quad p^2 \equiv (x^2, y^2, z^2, w^2).$$

## Mixture Diff. Cryptanalysis – 1st Case (2/2)

Given  $p^1, p^2 \in \mathcal{C}_0 \oplus a$  as before:

$$p^1 \equiv (x^1, y^1, z^1, w^1) \quad \text{and} \quad p^2 \equiv (x^2, y^2, z^2, w^2)$$

it follows that

$$R^4(p^1) \oplus R^4(p^2) \in \mathcal{M}_J \quad \text{if and only if} \quad R^4(\hat{p}^1) \oplus R^4(\hat{p}^2) \in \mathcal{M}_J$$

where

$$\hat{p}^1 \equiv (x^2, y^1, z^1, w^1), \quad \hat{p}^2 \equiv (x^1, y^2, z^2, w^2);$$

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## Mixture Diff. Cryptanalysis – 2nd Case

Given  $p^1, p^2 \in \mathcal{C}_0 \oplus a$  as before:

$$p^1 \equiv (x^1, y^1, z^1, w) \quad \text{and} \quad p^2 \equiv (x^2, y^2, z^2, w)$$

it follows that

$$R^4(p^1) \oplus R^4(p^2) \in \mathcal{M}_J \quad \text{if and only if} \quad R^4(\hat{p}^1) \oplus R^4(\hat{p}^2) \in \mathcal{M}_J$$

where

$$\begin{aligned} \hat{p}^1 &\equiv (x^1, y^1, z^2, \Omega), & \hat{p}^2 &\equiv (x^2, y^2, z^2, \Omega); \\ \hat{p}^1 &\equiv (x^2, y^1, z^1, \Omega), & \hat{p}^2 &\equiv (x^1, y^2, z^2, \Omega); \\ \hat{p}^1 &\equiv (x^1, y^2, z^1, \Omega), & \hat{p}^2 &\equiv (x^2, y^1, z^2, \Omega); \\ \hat{p}^1 &\equiv (x^1, y^1, z^2, \Omega), & \hat{p}^2 &\equiv (x^2, y^2, z^1, \Omega); \end{aligned}$$

where  $\Omega$  can take any value in  $\mathbb{F}_{2^8}$ .

## Mixture Diff. Cryptanalysis – 3rd Case

Given  $p^1, p^2 \in \mathcal{C}_0 \oplus a$  as before:

$$p^1 \equiv (x^1, y^1, z, w) \quad \text{and} \quad p^2 \equiv (x^2, y^2, z, w)$$

it follows that

$$R^4(p^1) \oplus R^4(p^2) \in \mathcal{M}_J \quad \text{if and only if} \quad R^4(\hat{p}^1) \oplus R^4(\hat{p}^2) \in \mathcal{M}_J$$

where

$$\begin{aligned} \hat{p}^1 &\equiv (x^1, y^1, z, \Omega), & \hat{p}^2 &\equiv (x^2, y^2, z, \Omega); \\ \hat{p}^1 &\equiv (x^2, y^1, z, \Omega), & \hat{p}^2 &\equiv (x^1, y^2, z, \Omega); \end{aligned}$$

where  $z$  and  $\Omega$  can take any value in  $\mathbb{F}_{2^8}$ .



## Reduction to 2 Rounds AES

Since

$$\text{Prob}(R^2(x) \oplus R^2(y) \in \mathcal{M}_J \mid x \oplus y \in \mathcal{D}_J) = 1$$

we can **focus** only on the **two initial rounds**:

$$\mathcal{C}_I \oplus b \xrightarrow{R^2(\cdot)} \mathcal{D}_J \oplus a' \xrightarrow[\text{prob. 1}]{R^2(\cdot)} \mathcal{M}_J \oplus b'$$

Consider  $p^1, p^2 \in \mathcal{C}_I \oplus a$ . We are going to prove that

$$R^2(p^1) \oplus R^2(p^2) \in \mathcal{D}_J$$

if and only if

$$R^2(\hat{p}^1) \oplus R^2(\hat{p}^2) \in \mathcal{D}_J,$$

where  $\hat{p}^1, \hat{p}^2 \in \mathcal{C}_I \oplus a$  are defined as before.

## Reduction to 2 Rounds AES

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**if and only if**

$$R^2(\hat{p}^1) \oplus R^2(\hat{p}^2) \in \mathcal{D}_J,$$

where  $\hat{p}^1, \hat{p}^2 \in \mathcal{C}_I \oplus a$  are defined as before.

## Idea of the Proof

Given  $p^1, p^2$  and  $\hat{p}^1, \hat{p}^2$  in  $\mathcal{C}_0 \oplus \mathfrak{a}$  as before, **if**

$$R^2(p^1) \oplus R^2(p^2) = R^2(\hat{p}^1) \oplus R^2(\hat{p}^2)$$

*then the previous result*

$$R^2(p^1) \oplus R^2(p^2) \in \mathcal{D}_J \quad \text{iff} \quad R^2(\hat{p}^1) \oplus R^2(\hat{p}^2) \in \mathcal{D}_J$$

*follows immediately!*

## Super-Box Notation (1/2)

Let  $super-SB(\cdot)$  be defined as

$$super-SB(\cdot) = S-Box \circ ARK \circ MC \circ S-Box(\cdot).$$

2-round AES can be rewritten as

$$R^2(\cdot) = ARK \circ MC \circ SR \circ super-SB \circ SR(\cdot)$$

## Super-Box Notation (2/2)

By simple computation,

$$R^2(p^1) \oplus R^2(p^2) = R^2(\hat{p}^1) \oplus R^2(\hat{p}^2)$$

is equivalent to

$$\text{super-SB}(P^1) \oplus \text{super-SB}(P^2) = \text{super-SB}(\hat{P}^1) \oplus \text{super-SB}(\hat{P}^2),$$

where

$$P^i \equiv SR(p^i), \hat{P}^i \equiv SR(\hat{p}^i) \in SR(C_i) \oplus a' \equiv \mathcal{ID}_i \oplus a'$$

for  $i = 1, 2$ .

## Sketch of the Proof (1/2)

Given  $P^1 = SR(p^1), P^2 = SR(p^2) \in \mathcal{ID}_0 \oplus \mathcal{a}'$ , note that

$$P^1 = \mathcal{a}' \oplus \begin{bmatrix} x^1 & 0 & 0 & 0 \\ 0 & 0 & 0 & y^1 \\ 0 & 0 & z^1 & 0 \\ 0 & w^1 & 0 & 0 \end{bmatrix}, \quad P^2 = \mathcal{a}' \oplus \begin{bmatrix} x^2 & 0 & 0 & 0 \\ 0 & 0 & 0 & y^2 \\ 0 & 0 & z^2 & 0 \\ 0 & w^2 & 0 & 0 \end{bmatrix}$$

## Sketch of the Proof

Since

- each column depends on different and independent variables;
- the super-SB works independently on each column;
- the XOR-sum is commutative;

then

$$\text{super-SB}(P^1) \oplus \text{super-SB}(P^2) = \text{super-SB}(\hat{P}^1) \oplus \text{super-SB}(\hat{P}^2)$$

for each  $\hat{P}^1$  and  $\hat{P}^2$  obtained by mixing/swapping the columns of  $P^1$  and  $P^2$ , e.g.

$$\hat{P}^1 = a' \oplus \begin{bmatrix} x^2 & 0 & 0 & 0 \\ 0 & 0 & 0 & y^1 \\ 0 & 0 & z^1 & 0 \\ 0 & w^1 & 0 & 0 \end{bmatrix}, \quad \hat{P}^2 = a' \oplus \begin{bmatrix} x^1 & 0 & 0 & 0 \\ 0 & 0 & 0 & y^2 \\ 0 & 0 & z^2 & 0 \\ 0 & w^2 & 0 & 0 \end{bmatrix}$$

## Mixture Diff. Distinguisher on 4-round AES

Consider  $p^1 \equiv (x^1, y^1, z^1, w^1)$ ,  $p^2 \equiv (x^2, y^2, z^2, w^2) \in \mathcal{C}_0 \oplus a$  s.t.

$$c^1 \oplus c^2 \equiv R^4(p^1) \oplus R^4(p^2) \in \mathcal{M}_J,$$

i.e.  $c^1$  and  $c^2$  are equal in  $4 - J$  anti-diagonals.

*Given  $\hat{p}^1, \hat{p}^2 \in \mathcal{C}_0 \oplus a$  obtained by mixing/swapping the generating variables of  $p^1, p^2$ , then:*

- 4-round AES: the event  $R^4(\hat{p}^1) \oplus R^4(\hat{p}^2) \in \mathcal{M}_J$  occurs with **prob. 1**;
- Random Perm.: the event  $\Pi(\hat{p}^1) \oplus \Pi(\hat{p}^2) \in \mathcal{M}_J$  occurs with **prob.  $2^{-32 \cdot (4 - |J|)}$** ;

**independently of the secret-key.**



# Distinguishers on 4-round AES

In bold, our new distinguisher for 4-round AES: they are all **independent** of the secret key!

<b>Data (CP/CC)</b>	<b>Complexity</b>	<b>Property</b>
4 CP + 4 ACC	4 XOR	Yoyo [RBH17]
$2^{16.25}$	$2^{31.5}$ M	Impossible Diff. [ <b>BK00</b> ] <b>Mixture Diff.</b> Integral [ <b>DLR97</b> ]
<b><math>2^{17}</math></b>	<b><math>2^{23.1}</math> M <math>\approx 2^{16.75}</math> E</b>	
$2^{32}$	$2^{32}$ XOR	

20 M  $\approx$  1-round Encryption

## Part III

# New Key-Recovery Attacks for AES

# Mixture Diff. Distinguisher + Key-Recovery Attack

Since

$$a \oplus \begin{bmatrix} x & 0 & 0 & 0 \\ 0 & y & 0 & 0 \\ 0 & 0 & z & 0 \\ 0 & 0 & 0 & w \end{bmatrix} \xrightarrow{R(\cdot)} b \oplus MC \times \begin{bmatrix} \text{S-Box}(x \oplus k_{0,0}) & 0 & 0 & 0 \\ \text{S-Box}(y \oplus k_{1,1}) & 0 & 0 & 0 \\ \text{S-Box}(z \oplus k_{2,2}) & 0 & 0 & 0 \\ \text{S-Box}(w \oplus k_{3,3}) & 0 & 0 & 0 \end{bmatrix},$$

the relations among the generating variables of  $R(p^1)$ ,  $R(p^2)$  and of  $R(\hat{p}^1)$ ,  $R(\hat{p}^2)$  depend on the key.

Idea of the attack:

$$\mathcal{D}_0 \oplus a \xrightarrow[\text{key guessing}]{R(\cdot)} \mathcal{C}_0 \oplus b \xrightarrow[\text{distinguisher}]{R^4(\cdot)} \text{Mixture Diff. Property}$$

where *the mixture differential property holds only for the secret-key!*

# Mixture Diff. Distinguisher + Key-Recovery Attack

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## Mixture Diff. Key-Recovery Attack (1/2)

Consider  $2^{32}$  chosen plaintexts with one active diagonal, that is  $p^i \in \mathcal{D}_0 \oplus a$  for  $i = 1, \dots, 2^{32}$ .

Find a pair of plaintexts  $(p, p')$  s.t. the corresponding ciphertexts after 5-round ( $c = R^5(p), c' = R^5(p')$ ) satisfy the property

$$c \oplus c' = R^5(p) \oplus R^5(p') \in \mathcal{M}_J$$

for a certain  $J$ , i.e.  $c$  and  $c'$  are equal in  $4 - |J|$  anti-diagonal(s).

## Mixture Diff. Key-Recovery Attack (2/2)

For each guessed value of  $(k_{0,0}, k_{1,1}, k_{2,2}, k_{3,3})$ :

- *partially* compute 1-round encryption of  $R(p), R(p')$  w.r.t. the **guessed-key**;
- let  $q, q'$  be two texts obtained by swapping the generating variables of  $R(p), R(p')$ ;
- *partially* compute 1-round decryption of  $\hat{q} \equiv R^{-1}(q), \hat{q}' \equiv R^{-1}(q')$  w.r.t. the *guessed-key*;
- if

$$R^5(\hat{q}) \oplus R^5(\hat{q}') \notin \mathcal{M}_J,$$

then the guessed key is wrong (where  $R^5(\cdot)$  is computed under the **secret-key**).

# Key-Recovery Attacks on 5-round AES-128

Property	Data ( $CP/CC$ )	Cost ( $E$ )	Memory
MitM [Der13]	8	$2^{64}$	$2^{56}$
Imp. Polytopic [Tie16]	15	$2^{70}$	$2^{41}$
Partial Sum [Tun12]	$2^8$	$2^{38}$	small
Integral (EE) [DR02]	$2^{11}$	$2^{45.7}$	small
<b>Mixture Diff.* [BDK+18]</b>	<b><math>2^{22.25}</math></b>	<b><math>2^{22.25}</math></b>	<b><math>2^{20}</math></b>
Imp. Differential [BK01]	$2^{31.5}$	$2^{33} (+ 2^{38})$	$2^{38}$
Integral (EB) [DR02]	$2^{33}$	$2^{37.7}$	$2^{32}$
<b>Mixture Diff.</b>	<b><math>2^{33.6}</math></b>	<b><math>2^{33.3}</math></b>	<b><math>2^{34}</math></b>

\*  $\equiv$  follow-up work

At Crypto 2018, Bar-On et al. [BDK+18] present the best (mixture-differential) attacks on 7-round AES-192 which use *practical* amounts of data and memory.

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## Part IV

# Concluding Remarks

# Future Open Problems

**Mixture Differential Cryptanalysis:** *a way to translate the (complex) “multiple-of-8” 5-round distinguisher into a simpler and more convenient one.*

## Future Open Problems:

- apply Mixture Differential on Tweakable AES-like ciphers: how many rounds can we break in related-tweak mode?
- is it possible to extend Mixture Differential distinguisher on 5 (or even more) rounds of AES? E.g.:
  - what about Mixture Differential in boomerang-/yo-yo-like attacks?
  - what about an “Impossible Mixture Differential Cryptanalysis”? (see <http://eprint.iacr.org/2017/832>)

## Just Keep an Open Mind!

*“Multiple-of-8” property hard to exploit directly for “practical applications”... however in less than 2 years it leads to*

- *new competitive distinguisher/attacks on round-reduced AES (e.g. Mixture Diff. Cryptanalysis and corresponding attacks proposed at Crypto 2018);*
- *new direction of research (e.g. next talk: “A General Proof Framework for Recent AES Distinguishers” by Boura *et al.*) and new unpublished results.*

*Do not limit ourselves to maximize the number of rounds that can be broken using known techniques:*

*also look for new directions in cryptanalysis that do not reach their full potential yet.*

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Thanks for your attention!

Questions?

Comments?

# References I



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